Algebra 2 – UNIT 5 Statistics and Probability

Critical Area:

Students analyze data to make sound statistical decisions based on probability models. By investigating examples of simulations of experiments and observing outcomes of the data, students gain an understanding of what it means for a model to fit a particular data set. Students develop a statistical question in the form of a hypothesis (supposition) about a population parameter, choose a probability model for collecting data relevant to that parameter, collect data, and compare the results seen in the data with what is expected under the hypothesis. Students build on their understanding of data distributions to help see how the normal distribution uses area to make estimates of frequencies (which can be expressed as probabilities). In addition, they can learn through examples the empirical rule, that for a normally distributed data set, 68% of the data lies within one standard deviation of the mean, and that 95% are within two standard deviations of the mean.

CLUSTERS	COMMON CORE STATE STANDARDS	
(s)Summarize, represent, and interpret data on a single count or measurement data.	Statistics and Probability – Interpreting Categorical and Quantitative DataS.ID.4. Use the mean and standard deviation of a data set to fit it to a normal distribution and to estimatepopulation percentages. Recognize that there are data sets for which such a procedure is not appropriateUse calculators, spreadsheets, and tables to estimate areas under the normal curve.	
Understand and evaluate random processes underlying statistical experiments.	 Statistics and Probability – Making Inferences and Justifying Conclusions S.IC.1. Understand statistics as a process for making inferences to be made about population parameters based on a random sample from that population. S.IC.2. Decide if a specified model is consistent with results from a given data-generating process, e.g., using simulation. For example, a model says a spinning coin falls heads up with probability 0.5. Would a result of 5 tails in a row cause you to question the model? 	
Make inferences and justify conclusions from sample surveys experiments, and observational studies.		
Use probability to evaluate outcomes of decisions.	 Statistics and Probability – Using Probability to Make Decisions S.MD.6. (+) Use probabilities to make fair decisions (e.g., drawing by lots, using a random number generator). S.MD.7. (+) Analyze decisions and strategies using probability concepts (e.g., product testing, medical testing, pulling a hockey goalie at the end of a game). 	

	MATHEMATICAL PRACTICES		
1.	Make sense of problems and persevere in		
	solving them.		
2.	Reason abstractly and quantitatively.		
3.	Construct viable arguments and critique	Emphasize MP 1, 2, 3, 4, 5, 6, and 7 in this unit.	
	the reasoning of others.		
4.	Model with mathematics.		
5.	Use appropriate tools strategically.		
6.	Attend to precision.		
7.	Look for and make use of structure.		
8.	Look for and express regularity in repeated		
	reasoning.		
LEARNING PROGRESSIONS			
Draft High School Progression on Statistics and Probability			
http://commoncoretools.me/wp-content/uploads/2012/06/ccss_progression_sp_hs_2012_04_21_bis.pdf			

(m) Major Clusters – area of intensive focus where students need fluent understanding and application of the core concepts.

(S) Supporting/Additional Clusters – designed to support and strengthen areas of major emphasis/expose students to other subjects.

***** Indicates a modeling standard linking mathematics to everyday life, work, and decision-making.

(+) Indicates additional mathematics to prepare students for advanced courses.

	ENDURING UNDERSTANDINGS		ESSENTIAL QUESTIONS	KEY VOCABULARY
•	In real life, data sets are large and almost always	٠	Why do we study normal distributions?	Bell curve
	approximately normal. Normal models which	•	Why is random sampling of a population done	bias
	include estimation of areas under the normal curve		when a census is impractical?	categorical data
	allow us to answer and model real life situations.	•	Do experimental probabilities match theoretical	census
•	Sampling methods, when highly representative of a		probabilities?	complementary events
	population, allow accurate predictions or inferences	•	How can a researcher select a method of	conditional probability
	of population parameters.		collecting data with as little bias as possible?	confidence interval
•	Students model probabilities found in experimental	•	How does the mean or proportion of a sample	convenience sample
	environment and decide whether they are consistent		compare to the mean or proportion of the	correlation coefficient
	with theoretical probabilities?		population?	counting methods
•	The mean or proportion of a sample is the same as	•	When does a statistic become extraordinary	critical value of z
	the mean or proportion of a population, within a		instead of ordinary?	distribution
	margin of error.	•	How do you know when the difference between	experimental probability
•	If the difference between the statistics of two		two treatments is statistically significant.	experimental study

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ENDURING UNDERSTANDINGS	ESSENTIAL QUESTIONS	KEY VOCABULARY
treatments is outside of a critical confidence	• There are many "studies out there", how do I	fairness
interval, the difference is statistically significant.	know if they are really accurate?	Histogram
• Select a method of gathering data from a random	• How can probability be used to make fair	independence
sample and understand data by critically	decisions?	independent events
differentiating the merit of reports and data		margin of error
encountered in daily life.		mean (x-bar)
• Probability can be used to develop strategies and		normal model or normal distribution
make informed decisions.		null hypothesis
		Numerical data
		observational study
		parameter
		population
		probability distribution
		proportion (p-hat)
		qualitative data
		random number generator
		random sample
		random variable
		representative sample
		sampling
		significant (as in statistics)
		simple random sample
		standard deviation
		statistic
		stratified random sample
		Subject
		survey
		systematic random sample
		theoretical probability
		treatment
		voluntary sample
		Z-Score

RESOURCES	INSTRUCTIONAL STRATEGIES	ASSESSMENT
LAUSD Adopted Textbooks and Programs	Engage students in a discussion or activity to clearly	
• <u>Big Ideas Learning - Houghton Mifflin</u> <u>Harcourt, 2015: Big Ideas Algebra 2</u>	distinguish between categorical and numerical variables by providing multiple examples of each	LAUSD ASSESSMENT
 <u>College Preparatory Mathematics, 2013: Core</u> <u>Connections, Algebra 2</u> <u>The College Board, 2014:Springboard Algebra 2</u> 	type. Have students practice their understanding of the different types of graphs for categorical and numerical variables by constructing statistical	The district will be using the SMARTER Balanced Interim Assessments. Teachers would use the Interim Assessment Blocks (IAB) to monitor the
Illustrative Mathematics:	posters. Note that a bar graph for categorical data may have frequency on the vertical (student's sport	progress of students. Each IAB can be given twice to show growth over time.
School Advisory Panel: S-IC.1 http://www.illustrativemathematics.org/illustrations/	preferences) or measurement on the vertical (students' grade in a test).	State Assessments
<u>186</u>	One tool for developing statistical models is the use	California will be administering the SMARTER Balance Assessment as the end of course for grades
Strict Parents: S-IC.1, 3 http://www.illustrativemathematics.org/illustrations/	of simulations. This allows the students to visualize the model and apply their understanding of the	3-8 and 11. There is no assessment for Algebra 1. The 11th grade assessment will include items from
122	statistical process. Provide students the opportunities to distinguish between a population parameter which	Algebra 1, Geometry, and Algebra 2 standards. For examples, visit the SMARTER Balance
Musical Preferences: S-IC.1, S-ID.5 <u>http://www.illustrativemathematics.org/illustrations/</u>	is a constant, and a sample statistic which is a variable. Use teacher-guided comparison	Assessment at: http://www.smarterbalanced.org/
123	conversations to ensure that students are able to make connections.	
SAT Score: S.ID.4 http://www.illustrativemathematics.org/illustrations/ 216	As the statistical process is being mastered by students, it is important for them to investigate	
Do You Fit In This Car?: S.ID.4 http://www.illustrativemathematics.org/illustrations/ 1020	questions such as "If a coin spun five times produces five tails in a row, could one conclude that the coin is biased toward tails?"	
Should We Send Out a Certificate?: S.ID.4 http://www.illustrativemathematics.org/illustrations/ 1218	Students will need to use all of the data analysis, statistics, and probability concepts covered to date to develop a deeper understanding of inferential reasoning. Have students critique published surveys before having them design their own surveys. Unlike	

	in observational studies; in surveys, the sample						
	selected from a population needs to be representative						
	of the population. Taking a random sample is						
generally what is done to satisfy this requirement.							
	Use a variety of devices as appropriate to carry out						
	simulations: number cubes, cards, random digit						
	tables, graphing calculators, computer programs.						
LANGUAGE GOALS for low a	achieving, high achieving, students with disabilities ar	nd English Language Learners					
	irposes of and differences among sample surveys, experi						
	chool students, more students are more/less likely to						
• Students will decide whether a specified model is							
<i>Example:</i> "A model stating that a spinning coin fa	alls heads up with a probability of 0.5 is not consistent wa	ith a simulation result of 5 tails in a row."					
	ey use statistical and probability concept in their lives, u	sing the following specific set of words: <i>distribution</i> ,					
mean, standard deviation, probability, and statist		a tast soons of is (- listing)					
	with a mean of and a standard deviation of under the normal curve allow us to answer and model rea						
• Students will explain orany and in writing areas u	inder the normal curve allow us to answer and model rea	i me situations.					
	PERFORMANCE TASKS						
Mathematics Assessment Projects (MARS Tasks)							
Modeling Conditional Probabilities 1: Lucky I	Dip: S.MD.6 <u>http://map.mathshell.org/materials/lessons.</u>	php?taskid=409&subpage=problem					
NCTM Illuminations Lessons							
- Should We Send a Cartificate? SID 4 http://www.illustrative.com/illustrative.com/1218							
Should We Send a Certificate?: S.ID.4 <u>http://www.illustrativemathematics.org/illustrations/1218</u> Full discrete the first of							
• Exploration with Chance: S.ID.6 <u>http://illuminations.nctm.org/LessonDetail.aspx?id=L290</u>							
Illuminations							
Fred's Fun Factory: S-MD.2, 5 and 7							
http://www.illustrativemathematics.org/illustrations/1197							
Miscellaneous Sources							
The Normal Distribution: S.ID.4 <u>http://www.wmich.edu/cpmp/1st/unitsamples/pdfs/C3U5_362-375.pdf</u>							

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DIFFERENTIATION					
UDL/FRONT LOADING	ACCELERATION	INTERVENTION			
Students should be encouraged to persevere when	S.MD.7 Apply this standard with more complex	Review the difference between independent			
problem solving in this unit. Multiple solutions are	probability models. You can implement the following	events and dependent events.			
 problem solving in this unit. Multiple solutions are common and should be recognized. Students can often make sense of complex contextual probabilities by considering a simpler analogous Probability situation (MP.1). As students work to identify events for which probabilities are to be determined and rules to apply, encourage students to verify and critique the thinking of their classmates (MP.3). Students have the opportunity to demonstrate proficiency with MP.6 by paying close attention to precise use of new vocabulary and writing complete sentences describing probabilities. 	 S.WD. / Appry this standard with hole complex probability models. You can implement the following activity: But mango is my favorite http://www.illustrativemathematics.org/illustrations/1333 Often two sample groups are compared in clinical studies. Two key criteria are specified: are the data normally distributed and are the data paired? Unpaired (independent) normally distributed data: Student's unpaired two-sample t-test For example, the efficacy of a new drug A may be compared with an established drug B. The study has 220 patients in treatment Group A with sample mean x̄A and standard deviation SDA and 200 patients in treatment Group B with sample mean x̄B and standard deviation SDB; (Group A and Group B do not have to be equal). We need to calculate the difference between the two sample means and the standard error of this difference between the two means, from which we can calculate a confidence interval for the difference between them. For t-test to be valid, the standard deviations of both groups must be similar. This is often the case, even when the sample means are significantly different. 	 Review the difference between independent events and dependent events. Review the conversions of: Ratios Percentages Decimals Teach students how to understand data in multiple forms: Graphs Charts Table Review key vocabulary words from previous sections 			

References:

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- 9. The University of Arizona. (2011-12). Progressions Documents for the Common Core Math Standards. Retrieved from http://ime.math.arizona.edu/progressions.